Two Nearest Means Method: Regression through Searching in the Data
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Abstract

Background: Historically, fitting a regression equation has been done through minimizing sum of squared residuals.  Investigators have to propose a model (main

Objective: We present an alternative approach that fits regression equations through searches for specific cases in the database. Case-based reasoning predicts outcomes based on matching to training cases and without modeling the relationship between features and outcome. This study compares the accuracy of the two nearest means (2NM), a search and case-based reasoning approach, to regression, a feature-based reasoning.

Data Sources: The accuracy of the two methods was examined in predicting mortality of 296,051 residents in Veterans Health Affairs nursing homes. Data was collected from 1/1/2000 to 9/10/2012. Data was randomly divided into training (90%) and validation (10%) samples.

Study Design: Cohort observational study.

Data Collection/Extraction Methods: In the 2NM algorithm, first data were transformed so that all features are monotonely related to the outcome. Second, all means that violate monotone order were set aside; to be processed as exceptions to the general algorithm. Third, for predicting a new case, the means in the training set are divided into “excessive” and “partial” means, based on how they match a new case. Fourth, the outcome for the new case is predicted as the average of two means: the excessive mean with minimum outcome and the partial mean with maximum outcome.

To evaluate, we predicted the accuracy of linear logistic regression and the proposed procedure in predicting mortality from age, gender, and 10 daily living disabilities.

Principal Findings: In cases set aside for validation, the 2NM had a McFadden Pseudo R-squared of 0.51. The linear logistic regression, trained on the same training sample and predicting to the same validation cases, had a McFadden Pseudo R-squared of 0.09. The 2NM was significantly more accurate (alpha <0.001) than linear logistic regression. A procedure is described for how to construct a non-linear regression that accomplishes the same level of accuracy as the 2NM.

Conclusions: 2NM, a Case-Based reasoning method, captured nonlinear interactions in the data.

Keywords: Case-Based Reasoning, K-Means, Algorithm, Disability, Prognosis, Veterans

Introduction

For decades, fitting an equation to data has been done through minimizing the sum of the squared residuals. Investigators have to propose a model (main
effects and interaction terms) and see how it fits the data. Unfortunately, in high dimensional data, it is not practical to specify all possible interactions and investigators need a deliberate way of finding the possible interaction terms. In this paper we provide an alternative method of organizing a regression model. This alternative approach works through searching the data for special cases. Because it is case-based reasoning, the approach takes into account all interactions within the data. Furthermore, the approach allows the examination of possible interaction terms prior to fitting a regression equation to data.

This proposed algorithm for regression is built on case-based reasoning. In case-based reasoning, one evaluates the entire case, including the interactions among the features in the case. The interactions among features are not explicitly modeled, although that can be done after the algorithm identifies the possible interactions. The outcome for the entire case is compared to outcomes of other cases. Case comparisons always include the interactions among the features. Since, by definition, a case is a collection of features, the process implicitly accounts for feature interactions. In contrast, feature-based reasoning, e.g., regression, uses the features in the case to evaluate the case, and interactions among the features are not modeled, unless the investigator specifies them. In high dimensional or massive data, case-based reasoning is preferred to feature-based algorithms because it is often computationally impractical to assess parameters for interactions among all features. In this paper, we describe a new case-based reasoning method and show how it can capture non-linearities missing in feature-based algorithms.

Methods

Conditions under which Algorithm Works

The proposed algorithm works in broad set of environments but requires a number of data transformation before applying the algorithm. A case is a collection of features \(X_1, \ldots, X_n\). The purpose of the algorithm is to predict the outcome \(Y\) for case \(P\), having features \(X_{1p}, \ldots, X_{np}\). Thus, \(Y(X=x)\) refers to the outcome for the case where the feature set \(X\) has the values in \(x\). We assume that all features, \(Z_i\), are either binary variables taking on values of 0 or 1 or are standardized to range between 0 and 1. To standardize \(Z_i\), the minimum-maximum transformation can be used:

\[
X_i = \frac{Z_i - \text{Min}(Z_i)}{\text{Max}(Z_i) - \text{Min}(Z_i)}
\]

We assume that all features \(X_i\) are arranged so that they are monotonely and positively related to \(Y\), the outcome of interest. Thus, if \(i > r\), then \(Y(X_i = j) \geq Y(X_r = r)\). If \(Z_i\) variables are not monotonely increasing, then these variables are revised so that they are:

- Non-monotone \(Z_i\) variables are split into two or more monotone \(X_i\) variables. For example, if age sometimes increases and other times decreases the outcome, then various age ranges are used as separate variables, so that within these ranges, the age variable always has the same effect on the outcome.
- \(Z_i\) features that are negatively related to the outcome are redefined to \(X_i\) so that they are positively related to the outcome. For example, if the outcome of interest decreases among male gender (defined as male=1, female=0), then the gender feature is redefined to be female (i.e., female=1, male=0).

In our algorithm, the training data are classified into \(m\) Means. In our terminology, a Mean refers to the average outcome, \(Y\), calculated over a set of cases with same features. It is important to have as many Means in the training data as possible, as the number of Means and the range of outcomes for the Means determines the accuracy of the predictions in our procedure. At the same time, too few cases per Mean reduces the precision of the estimated outcome for the Mean and therefore reduces the accuracy of predictions. The analyst needs to strike a balance between number of Means and number of cases per Mean. If all case features, including the outcome \(Y\), are binary, then the outcome for Means is reported as the probability of \(Y\). Usually, at least 30 repeated cases in the training data are used to identify the Mean and its probability. As the size of training data increases, using a minimum of 30 cases per Mean leads to identification of more Means. We selected 30 cases as a minimum number for a stable Mean because around 30, the Binomial distribution can be approximated by Normal distribution. If the data are not binary, the k-Means approach is used to identify as many Means as possible within the training data. Investigators often select the k-parameter in the k-Means by trial and error in the training set, to see what best fits the data [1-3]. Some authors have proposed that the k parameter should be chosen as a function of size of the data, with more Means chosen in bigger data [4]. Our approach is to use as large a \(K\) that fits the training data.

A Motivating Example

To help motivate the logic of the algorithm, we first present it in a simplified context of two variables: \(X_1\) and \(X_2\). Figure 1 shows that \(X_1\) and \(X_2\) are monotonely related to the outcome \(Y\), i.e., going from \(a_1\) to \(e_1\) on \(X_1\) and going from \(e_1\) to \(a_1\) on \(X_2\) do not lead to decreases in \(Y\). Figure 1 shows the 8 Means in the data shown with alphabets A through H. These Means differ in values of \(X_1\) and \(X_2\) and have different levels of outcome \(Y\) associated with each mean. The prediction task is to predict the outcome for a new case, shown as \(P\), with value \(p_1\) on \(X_1\) and value \(p_2\) on \(X_2\). The purely excessive set of Means are all the Means that have more of \(X_1\) or \(X_2\) than the case \(P\). In Figure 1, these are \(F\), \(G\), and \(H\), for example,
has more of both $X_1$ and $X_2$. Partial sets are all the Means that have less values of either $X_1$ or $X_2$. In Figure 1 these are $B$, $C$, and $D$. For example, $B$ has less of $X_1$ than case $P$ and same value on $X_2$ as case $P$.

A more complex situation arises when the Mean has some features less and other features more than the case $P$. The Mean $A$ is a mixed Mean, it has level $a_2$ on $X_2$, which exceeds $p_2$ for the case $P$. It has level $a_1$ on $X_1$, which is less than $p_1$ for case $P$. Similarly, Mean $E$ is a mixed Mean, compared to $P$, it exceeds on $X_1$ but is less on $X_2$. These mixed Means can belong to either partial or excessive category, depending on the net impact of Means where just $X_1$ and $X_2$ are present. If $Y(X_1 = 0, X_2 = a_2) > Y(X_1 = a_1, X_2 = 0)$, then Mean $A$ is classified as excessive because the impact of excess on $X_1$ is higher than the impact of loss on feature $X_1$. Similarly, Mean $E$ is assigned to excessive set if the net effect of having more of $X_1$ and less of $X_2$ is positive, i.e., $Y(X_1 = 0, X_2 = a_2) > Y(X_1 = a_1, X_2 = 0)$.

Once all Means are classified into partial and excessive sets, then the outcome for patient $P$ is bounded by the maximum outcome in the partial set and the minimum outcome in the excessive set. The middle of the upper and lower bound is an estimate of the outcome for case $P$.

**Figure 1: Partial and Excessive Sets in Matches to Patient P in Two Dimensions**

For a more clinical example, consider predicting mortality from two factors: severity of cardiac illnesses and severity of infectious diseases in the patient’s medical history. We agree that more severe illnesses lead to more mortality, thus the relationship is monotone. Suppose in a training set we have 8 types of patients, as in Figure 1, each with differing levels of cardiac and infectious illnesses. Suppose that a patient shows moderate levels of severity for both cardiac and infectious diseases. Then, $C$, $B$, and $D$ are partial types because they have at least one feature less severe than patient $P$ and no feature worse than patient $P$. Furthermore, $F$, $G$, and $H$ are excessive Means or types of patients as they have at least one feature that exceeds in severity than patient $P$ and no feature that is less severe. The patient types $A$ and $E$ are mixed types, as one feature indicates more severe and another less severe illness. These two mixed types are reclassified into excessive or partial types based on the relative severity of types with just cardiac and infectious diseases. Suppose, $A$ is classified as excessive and $E$ as partial. The algorithm calculates the probability of mortality for patient $P$ from the maximum of partial patient types, in this case, $E$ and the minimum of excessive patient types, in this case $A$.

Note that in these comparisons, we never used feature-based reasoning. We did not create a model, e.g., a regression equation, about how much features $X_1$ or $X_2$ contribute to the outcome $Y$. We also did not use Euclidian distance (squared root of sum of squared differences on each feature) between cases to judge the similarity of the cases. The entire inference was based on outcomes in various cases; we examined Means where $X_1$ or $X_2$ had different levels. The outcome for case $P$ was inferred from the outcome for Means in the training set of data, without calculating the contribution of each feature to the outcome.

**Description of the Algorithm**

This algorithm repeatedly uses a concept known in the literature as Preferential Independence to organize the data [5]. In preferential independence, shared features of a Mean do not affect the order of outcomes of the Means. If $S$ is a set of shared features and $N$ is a set of features not shared, then $Y(S = s, N = n)$ is the outcome for the Mean with shared features “$s$” and unshared features “$n$”. Preferential independence assumes that the order of outcomes for any two Means stays the same, independent of the shared features. Changing shared features “$s$” to “$t$” does not change the order of outcomes of the two Means:

$$Y(S = s, N = n) > Y(S = s, N = m) \equiv Y(S = t, N = n) > Y(S = t, N = m).$$

The monotone organization of features, discussed earlier, requires that a Mean with an added feature should not have a lower outcome. If $n$ indicates the feature set of the starting Mean, then monotone relationship requires:

$$n + 1 > n \equiv Y(S = n + 1, N = 0) \geq Y(S = n, N = 0).$$

Preferential independence allows us to generalize the monotone relationship to a variety of pairwise comparisons of Means. Our experience to date has shown that in almost all databases, the monotone relationship does not hold for all pairwise comparisons.

**Step 1: Remove Order Violations from the Training Set.** The first step in the algorithm is to remove Means in which adding a new feature violates the assumed monotone relationship. Violation of the required order identifies Means that are exceptions to the general model developed here to organize the data. These Means are not following the general pattern in the data and should be treated separately. If a new case matches the exceptions, then the model is ignored, and the outcome of the exceptional Mean is used to predict the
outcome for the new case. To identify the exceptions, these steps can be followed:

1. Using the training set of data, start with the Mean where no feature is present. Call this the reference Mean.
2. Add a feature to the reference Mean, creating a new Mean with an added feature than the starting Mean. We refer to these types of Means as “Excessive Mean.” Look up the outcome for the constructed Excessive Mean in the data.
3. Test if the pair of Means have an order violation, where the Mean with added feature has a lower outcome than the Mean without it. Small variations in data can be ignored as all data have random variations that violate order requirements. The purpose of searching for exceptions is to identify large and consistent order violations.
4. Repeat steps 2 and 3 until all pairs of Means have been examined.

The Means with the highest number of order violations are assigned to the Exception set. When an order violation is observed, it is not clear if the violation is due to the reference Mean having an unusually high outcome or the Excessive Mean having an unusually low outcome. We propose to focus on the Mean with the largest number of order violations.

**Step 2: Assign Means in Training Set to Excessive, Partial, and Mixed Sets.** To predict the outcome for a new case, the Means in the training data (excluding exceptions) are classified into three types: partial, excessive, or mixed. If there is a Mean that exactly matches every feature of the new case, then there is no need for the algorithm and the predicted value for the new case is the average of the Means in the Partial set.

**Step 3: Re-classify Mixed Means.** One classifies Means in $Y_\pm$ to either $Y_-$ or $Y_+$ based on two methods. If the classification of the Mean to Excessive set creates an order violation, then the Mean is classified as Partial. This occurs if the re-classified Excessive has an outcome that is lower than the highest outcome for Means in the Partial set. Also, the reverse holds: if the classification of the Mean to partial creates a new order violation, then it is classified as Excessive. This occurs if the re-classified Partial has an outcome that is higher than the lowest outcome of the Means in the Excessive set.

Not all re-classifications create order violations. If it is possible to reclassify the Mean to either Partial or Excessive without order violations, then one keeps the order of cases constructed from the mismatched features.

$$Y'(X_2 = s, X_p = p, X_e = e) \in Y^+ \iff Y'(X_2 = 0, X_p = e) > Y'(X_2 = 0, X_p = p)$$

In these situations, the order of the mixed case is decided based on what is known as “Corner Means.” An Excessive Corner Mean is composed of just the additional features in the mixed Mean and no other feature being present. A Partial Corner Mean is composed of only missing features in the mixed Mean and no other features. By preferential independence, the comparison of Excessive and Partial Corner Means establishes the assignment of the mixed Mean. Corner Means occur often and the order among them can be observed in the data. If this is not the case, these corner Means must be estimated through data balancing. An SQL code for estimate the net impact of Corner Means is available through the first author [6].

**Step 4: Estimate the Outcome for New Case.** The outcome for the new case is predicted as the average of the partial Means with the highest outcome and Excessive mean with the lowest outcome:

$$Y' = \left\{ \begin{array}{ll} \frac{\text{Maximum}(Y^-)}{2}, & \text{if } Y^+ \text{ is null} \\ \frac{1 + \text{Minimum}(Y^+)}{2}, & \text{if } Y^- \text{ is null} \\ \frac{\text{Minimum}(Y^-) + \text{Minimum}(Y^+)}{2}, & \text{otherwise} \end{array} \right.$$  

There are situations in which no partial or no excessive matches exist. These situations occur at border points, where there are no lower or upper bounds. If the partial set $Y^-$ is null, then 0 is assumed. If excessive set $Y^+$ is null, then 1 is assumed.

**Optimality of the Algorithm:** A mathematical proof of optimality can be found in Keeney and Raiffa [7], where they use mutual preferential independence to create a mathematical model that preserves order of outcomes. In such a model, the maximum of partial and the minimum of excessive Means are the closest Means to the new case. The assumption of preferential independence and monotone positive relationship between features and the outcome, implies that Means in the excessive set have higher outcome than the new case. If the Mean in the partial set has an outcome that exceeds the minimum of the excessive set, then preferential independence is violated. Therefore, the lowest outcome among the Means in the excessive set is the upper bound for the new case.
Similarly, the Mean with the maximum outcome in the partial set is closest to the outcome of the new case. Since these two Means have the outcomes closest to the new case, therefore the estimated average of maximum and minimum outcome for the new case is optimal.

**Identifying Interaction Terms**

Some investigators assign meaning to feature weights in regression equations. These investigators may want to examine feature weights, even if 2NM algorithm is available. These investigators can use the procedures of the 2NM algorithm to identify which interaction terms might affect the outcome variable, then derive the regression model with the interaction term. To find out what interactions may exist in the data, the data is transformed as proposed for application of 2NM algorithm, then preferential independence plots are created. These plots are organized by examining. The effect of a variable (present or absent) on the outcome, as a function of different shared features. One line is plotted for cases with the shared features. Another line is plotted for cases without the features. The X-axis is the shared features, plotted in order of increasing outcome. Two lines are plotted. The first line is the outcome for the case with just shared features and the variable being examined. The second line is the outcome for the case with shared features and the variable being examined. If there is no interaction term between the variable and the shared features, then the two lines must be parallel or nearly parallel throughout the range. Changing the shared features should not change the impact of the variable. If there is an interaction term in the data involving the variable, then the two lines could be diverging or converging. If the two lines cross each other then it indicates a violation of preferential independence. Preferential independence plots are reported in previous papers [8]. Preferential Independence plots show at what shared features there is a change in impact of a variable. Typically, a large number of interaction terms are identified and, for ease of use, the common denominator among the interaction terms is used. Once possible interaction terms have been identified, then a regression with the combination of main effects and interaction effects can capture the non-linearity in the data.

**Results**

**Simple Simulated Data**

We show the accuracy of predictions using a simulated data set with a single standardized variable X. We focus on a single-variable simulation because it is easier to visualize the performance of 2NM in a single variable than in a multiple-variable simulation. Let us assume that increases in X never decrease values of Y and X is positively and monotonely related to Y. Figure 2 shows such a simulated relationship. The observed data, shown in blue dots, shows that the values of Y either stay the same or increase as X increases. The black line shows the fit of a regression equation to the data. This fit is an optimal fit to the single feature in the simulation. The 2NM relies on case comparisons and in this simulation, the cases have only one variable. Thus, for any point in the data, the 2NM is calculated as the average of the point before and after it (the orange line). The $R^2$ associated with the fit of the regression line to the data was 0.85; in contrast the $R^2$ associated with the fit of 2NM was 0.88. The 2NM had a better fit, as it moved closer to the data points, when the relationship was not linear.

**Application to Real Data**

We tested the accuracy of predictions on a large database organized to guide what is likely to occur in a nursing home residents’ life. The outcome of interest was probability of death in the next 6 months. The sample included 296,051 residents in Veterans Affairs nursing homes called Community Living Centers (CLCs). The period of study included 1/1/2000 through 9/10/2012. These data included a comprehensive assessment of residents’ disabilities. Independent variables were gender (M), and whether the resident had feeding (E), bathing (B), grooming (G), dressing (D), bowel continence (L), bladder continence (U), toilet use (T), transfers (S), and walking (W) disabilities. To simplify, we show a combination of features present and assume that all features not mentioned were absent. Thus, MUE shows a male patient with urine continence and feeding disability. WB shows a female resident with walking and bathing disabilities. By policy, assessments were done within 14 days of admission, at least quarterly, or sooner when there has been an event such as hospitalization, or when the nursing home staff identify change in the resident’s status. In our data, there were two peaks in the distribution of assessments; one for residents assessed every month (75,994 residents) and the other for residents assessed every 3 months (42,904 residents). The average time between assessments was 115 days (standard deviation of 235 days).
The assessments were grouped into 1,346 unique combinations of functions and gender. The rare combination with less than 10 cases were ignored, resulting in 758 unique combinations of gender and disabilities, what in 2NM terminology is referred to as reliable Means. Ten percent of the data (67 cases) were set aside to test the accuracy of predictions. The remaining 90% were used for training of 2NM predictions and creating the reliable Means. The first step in the analysis is to check that the assumptions of 2NM are met, in particular we checked that for all Means in the training set adding another condition to the Mean does not reduce the probability of mortality. Table 1 lists situations where preferential independence was violated. Because of the large sample of data, we used both effect size (greater than 0.10 drop in the mortality rate) and statistical significance ($Z>1.98$). For example, in the first row in the table we see that adding “Grooming (G)” disability to “Older, Male, OM” patients with no disability will lead to a -0.66 drop in the mortality rate. Obviously, adding a disability should not reduce mortality rates and, in fact, out of 202 times where grooming disability was added to another condition only on 6 occasions the rate of mortality dropped. It almost always made the mortality rate worse. A quick analysis of Table 1 shows that violations of preferential independence occur mostly in patients who have no disabilities (shown as “males older than 74 years OM”, “females older than 74 years OF”, “males less than 65 years YM”, “females less than 65 years YF”, “males 65-74 years M”, “females 65-74 years F”). In addition, violations of preferential independence also occurred in older male patients with all disabilities present but not urine incontinence or toileting disability (shown as OMERGBWDL). These situations cannot be modeled with 2NM. We set aside these situations as exceptions and focused on portions of the data where there was no violation of preferential independence. This reduced the Means available in the training set from 688 to 681 Means. In the Means remaining in the training set, there were no large and statistically significant violations of preferential independence.

Examples shown in Table 2 demonstrate the way the 2NM prediction works. In a new case MGWD (a patient who is under 65 years, male, with grooming, walking, and dressing disabilities), we searched the database and found the closest partial and excessive Means. The 5 Means provided differ from MGWD by one feature. MGW, MWD, and MGD are partial matches. MGBWD and MGTWD are excessive matches. MGBWD is not possible as its mortality rate is lower than MGD, even though it has more disabilities. Thus, it violates the assumption of preferential independence. We ignore this Mean. Now we have a set of partial matches and another set of excessive matches. The maximum mortality rate for partial matches is MGD. The minimum mortality rate for excessive matches is MGTWD. Therefore, we predict that patient MGWD has a mortality rate of 0.025. In reality, it had a mortality rate of 0.015.

For patient MSGWDL (a patient who is under 65, male, with transfer, grooming, walking, dressing disabilities, and bowel incontinence), we follow the same procedure. The six Means identified differ from the patient by one feature. First, we remove Means that violate preferential independence: MRGTBWDL and MGBWDL. These two Means have more disabilities than MRGBWL but have lower mortality rate, a violation of preferential independence. The two nearest Means are MSGBWL, the maximum of partial set, and MRGBWDLU, the minimum of excessive set. For this patient, we predict a mortality rate of 0.018. The observed rate was 0.030. For our final example in Table 2, we have a patient OMWL (between 65 and 74 years, male, with walking disability and bowel incontinence). Again, the Mean MRGTBWDL is not possible as it has more features but lower mortality rate than OML. After eliminating this Mean, the maximum mortality rate for the partial set is OML and the minimum mortality rate for the excessive set belongs to OMWLU. Therefore, we predict this patient will have a mortality rate of 0.016 and in fact it had a mortality rate of 0.020.

In 130,428 set-aside validation cases, the 2NM had a McFadden Pseudo R-square of 0.51. A linear logistic regression was trained on the 1,174,218-training sample used by 2NM, using the linear combination of the same set of variables (age, gender, and disabilities). On the validation cases, the McFadden Pseudo R-squared for the linear logistic regression was 0.09.

**Discussion**

This paper shows that the optimal number of Means to use in k-Means methods is 2, if the data are transformed to fit a series of assumptions. These assumptions create a monotone positive relationship between the features and the outcome of interest. These assumptions also create a data set where the order of preferences among combination of features is the same in any subset of data. Data can be organized to meet these assumptions. Once the data are transformed to meet the assumptions of 2NM, then we divide Means into excessive and partial sets. Mixed Means (both partial and excessive) can be re-assigned based on the net impact of their partial and excessive feature sets. The maximum outcome of the partial and minimum outcome of the excessive Mean estimates the outcome for a new case. The procedure we used was accurate in a simple 1 variable simulation, showing how 2NM captures non-linear aspects of the data. We also compared 2NM and linear Logistic Regression in a large database of nursing home resident’s disabilities. In predicting 6-month mortality in 10% set aside test cases, 2NM was more accurate than linear Logistic regression (Pseudo R-square of 0.51 versus
This study reports accuracy of a new case-based reasoning method called Two Nearest Means (2NM). Unlike traditional methods such as k-means or Nearest Neighbor, which rely on feature-by-feature comparisons, 2NM considers the interaction among the features in their entirety. The linear regression model did not produce limited improvements in accuracy. In contrast, 2NM, closeness is measured on a single dimension: the outcome. The dimension is defined by the closeness of cases to a decision boundary.

Traditionally, Nearest Neighbor and k-Means have relied on a distance metric to predict the outcome for a new case. In this approach, one typically defines closeness based on the Euclidean distance calculated over all the features. Euclidian distance is arbitrary; one could have specified non-Euclidean measures of distance. Furthermore, the distance measure is often used with no regard for interaction among the features, a procedure known to reduce accuracy [9, 10]. Some investigators have tried to consider the non-linearity of the features by creating separate models for sub-classes in the data or through Kernel methods [11-13]. These efforts continue to weigh various features, albeit in new and novel ways but produce limited improvements in accuracy [14]. In contrast, in 2NM, closeness is measured on a single dimension: the outcome. The outcome is the only dimension where closeness matters, closeness in all other multidimensional spaces is irrelevant. By using feature-based measures of distance, Nearest neighbor and K-means undermine a key advantage in case-based reasoning. The approach presented here requires no feature weighting. It predicts purely through aggregate, case-based comparisons. The assignment of cases into exceptions, excessive, and partial is done entirely through contrasting outcomes in pairs of cases. Since cases reflect the interaction among the features, then 2NM considers the interaction among the features. It does not disaggregate the case into features and then uses a formula (typically only main effects) to re-combine the features into a distance measure. The 2NM procedure may be more relevant in high dimensional data, where it is often difficult to specify all interactions among the features. The proposed algorithm may improve accuracy because it relies on case comparisons without feature-by-feature comparisons.

Limitations of the Algorithm

For the algorithm to be accurate, the Means in the training set must have values in the entire range of possible outcomes. Sufficient data should exist to have a variety of Means, ranging in probability of outcome from 0 to 1. For example, if we are examining probability of mortality, then we should have Means, or group of cases, where no one dies; where everyone dies, and different mixtures in between these two extremes. In predicting the outcome for a new case, a dense, uniform, distribution of Means and their probability of the outcome guarantees that the two Nearest Means for the new case are close to each other and thus a more precise prediction can be made.

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What Is Known on This Topic?

- Case-based reasoning, such as k-means or Nearest Neighbor, take into account interactions among the features of the case, except when measuring distance among cases.
- Accuracy of case-based reasoning and feature-based predictions are similar

What This study Adds?

- This study reports accuracy of a new case-based reasoning method that does not rely on feature-based distance calculations.

References


